MARKET SEGMENT EVALUATION AND SELECTION BASED ON APPLICATION OF FUZZY AHP AND COPRAS-G METHODS

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Abstract. Market segment evaluation and selection is one of the critical marketing problems of all companies. This paper presents a novel approach which integrates fuzzy analytic hierarchy process (FAHP) and COPRAS-G method for market segment evaluation and selection. Fuzzy AHP is used to calculate the weight of each criterion, and COPRAS-G method is proposed to prioritize market segments from the best to the worst ones. The application of fuzzy set theory allows incorporating the vague and imprecise linguistic terms into the decision process. This study can be used as a pattern for market segment selection and future researches. A case study on a chair manufacturing company is put forward to illustrate the performance of the proposed methodology.

Keywords: market segmentation, market segment evaluation, market segment selection, Fuzzy AHP, COPRAS-G method.


JEL Classification: C02, C44, D40, D46, D81.

1. Introduction

Market segmentation becomes an essential element of marketing in industrialized countries and in living of any business (Wedel, Kamakura 2000). Market segmentation is defined as the partitioning of a market into distinct subsets of customers and any subset could be possibly selected as a target market to be reached with a distinct marketing mix (Kotler 1999). In other words, market segmentation makes it possible to find homogeneous smaller markets by this means, helping marketers to recognize marketing opportunities and to develop products and services in a more tailor-made manner (Jang et al. 2002).
Although market segmentation was introduced into the academic marketing literature by Smith (1956), market segmentation continues to be an important focal point of ongoing research and marketing practices (Chaturvedi et al. 1997; Hanafizadeh, Mirzazadeh 2011). Maybe mass marketing will no longer exist in the coming century or it will become vanished (Kuo et al. 2002). There are a lot of advantages of market segmentation over mass marketing. Firstly, it repeatedly helps every company to find a good chance to expand its own market by better satisfying the wants of customers. Secondly, it increases the profitability or effectiveness of the organization to the extent that the economic benefits provided for consumers exceed the costs of the segmentation process (Chiu et al. 2009). Thirdly, the importance of doing marketing segmentation analysis includes better perception of the market to truly position of a product in the marketplace, choosing the appropriate segments for target marketing, discovering opportunities in existing markets, and gaining competitive advantage through product differentiation (Kotler 1980).

There are many market segmentation bases in the literature that were used to divide a market into segments such as geographic, demographic, life style and product benefits (Kazemzadeh et al. 2009). Besides, there are numerous market segmentation methods such as factor analysis, clustering, conjoint, regression, and discriminate analysis. Also recently, using or integrating other fields including data mining, multivariate statistical analysis, fuzzy logic, artificial neural networks, and genetic algorithm becomes a common tool for market segmentation.

After market segmentation, every company needs to evaluate and select target market or markets, and then Market segmentation evaluation is a critical management decision because all other components of a marketing strategy follow it (Wind, Thomas 1994). Also, Market segment evaluation can help in targeting markets, thus it is very important for improving the probability of success in competitive market.

Although much of the marketing literature has proposed various market segmentation techniques, but a review of academic research reveals that existing studies have relatively neglected segment evaluation and selection (Sarabia 1996; Ou et al. 2009). Also most existing studies suggest some general criteria for evaluation of attractiveness of a segment and merely present a model or method for evaluation.

Selecting an appropriate market segment based on evaluation of segments is one of the most complicated and time consuming problems for many companies, due to many feasible alternatives, conflicting objectives and variety of factors (Aghdaie et al. 2011). Market segment evaluation and selection decisions are sophisticated by the fact that the decision-making process must consider various criteria. Therefore market segment evaluation and selection can be viewed as a multiple criteria decision-making (MCDM) problem. Hence, this study has the main objective of proposing a mechanism for market segment evaluation and selection.

The MCDM methods deal with the process of making decisions for finding the optimum alternative in the presence of multiple, usually conflicting, decision criteria.

In this research a hybrid MCDM model encompassing fuzzy analytic hierarchy process (FAHP) and the complex proportional assessment of alternatives with grey relations
(COPRAS-G method) are used for market segment evaluation and selection. Specifically, FAHP is initially used for calculating the weight of each criterion and COPRAS-G method is used for ranking and selecting the best location.

The remainder of this paper is organized as follows. The related studies are summarized in Section 2. The third section presents the methodology including FAHP and COPRAS-G method. In Section 4, a real-world case study is given to prove the applicability of the proposed method on a large-sized manufacturing enterprise in Iran. In Section 4, the results are discussed. In Section 5, finally, the article will be concluded.

2. Literature review

Market segment evaluation and selection is one of the important problems for every company. The major part of the related literature concentrates on the important features for doing this evaluation and very little research has been done on the evaluation of segment attractiveness and market segment selection. The enormous majority of decision-making methods identified apply to the final stage of market segment evaluation and selection. Also, it is remarkable that segmentation itself has many limitations in terms of product, segment size, profitability/yield, attainability with promotion mix and supply, doubled expenses for marketing mix, industry, etc. Generally, expert efforts have focused on evaluating different segmentation methods and techniques (Bonoma, Shapiro 1983; Christen 1987; Elrod, Winner 1982; Morrison 1973; Novak et al. 1992; Wildt 1976). Even general studies of market segmentation have paid little or no attention to the evaluation and selection stages (Beane, Ennis 1987; Weinstein 1987; Wind 1978). Authors generally limit themselves to analyzing how to evaluate segment stability (Bettman 1971; Calentone, Sawyer 1978; Lehmann et al. 1982; MacLachlan, Johansson 1981), congruence (Green 1977), internal homogeneity and profitability (Eckrich 1984; Van Auken, Lonial 1984; Beik, Buzby 1973), to mention only the most relevant.

Some general criteria such as identity ability, substantiality, accessibility, stability, responsiveness, action ability have been frequently put forward as determining the effectiveness and profitability of market segment (Frank et al. 1972; Loudon, Della Bitta 1984; Baker 1988; Kotler 1988). Based on research of the United Kingdom’s Times Top 1000 companies, Simkin and Dibb (1998) found that the three most important factors for selecting target markets were profitability, market growth, and market size. McQueen and Miller (1985) recommended the assessment of market attractiveness based upon profitability, variability, and accessibility. In the same way, Loker and Perdue (1992) proposed a systematic approach to evaluating segments using a ranking procedure. They assessed segment attractiveness in terms of profitability, accessibility, and reachability by ranking each segment on its relative performance according to the three evaluation criteria. Based on Kotler and Armstrong (2003) the market segments should meet five selection criteria including: (1) measurable, (2) accessible, (3) sustainable, (4) differentiable, and (5) actionable to be viable. Also, Morrison (2002) added five more criteria in Kotler and Armstrong’s list for effective segmentation, including: homogeneity, defensibility, competitiveness, durability, and compatibility. These theoretically fundamental
criteria provide marketers with useful guidelines for targeting markets (Lee et al. 2006). Bock and Uncles (2002) suggested that, when preparing a segmentation strategy, profitability must be considered as one of the main selection criteria. Jang et al. (2002) incorporated the profitability and risk concepts in evaluating segment attractiveness as more quantifiable and comprehensive profitability measures. Most of these studies, propose different schemes for market segmentation, however, they have concentrated on evaluation and therefore have only taken into account very specific criteria. Ou et al. (2009) incorporated the famous model that was developed by Porter (1980) to evaluate each potential segment. Companies must carefully assess and weigh key discriminating criteria to find the “best” market segments (Weinstein 2004).

McDonald and Dunbar (2004) prepared one of the comprehensive criteria list for market segment evaluation. They also provide a list of twenty-seven possible, generalized segment attractiveness factors in five major areas: segment factors, competition, financial and economic factors, technology, and sociopolitical factors. McDonald and Dunbar add segment attractiveness factors be weighted based on the particular requirements of an organization.

This study uses the McDonald and Dunbar’s (2004) criteria list as the basis for market segment evaluation. This criteria list is depicted in Table 1.

<table>
<thead>
<tr>
<th>Table 1. The segment attractiveness criteria</th>
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<tbody>
<tr>
<td>Criteria</td>
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<td>---------------------------</td>
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<tr>
<td>Segment factors</td>
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<tr>
<td>Financial and economic factors</td>
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</table>
3. Methodology

Over the past decades the complexity of economic decisions has increased rapidly, thus highlighting the importance of developing and implementing sophisticated and efficient quantitative analysis techniques for supporting and aiding economic decision-making (Zavadskas, Turskis 2011). Multiple criteria decision making (MCDM) is an advanced field of operations research, provides decision-makers and analysts with a wide range of methodologies, which are overviewed and well suited to the complexity of economic decision problems (Hwang, Yoon 1981; Zopounidis, Doumpos 2002; Figueira et al. 2005). In this paper, we proposed a combined fuzzy AHP and COPRAS-G method approach to market segment evaluation and selection. The evaluation criteria for market segment evaluation and selection are based on McDonald and Dunbar’s (2004) criteria list. According to these criteria, the required data utilized in the comparisons are collected from the related decision makers (DMs). After constructing the evaluation criteria hierarchy, the criteria weights are calculated by applying the fuzzy AHP method. Finally COPRAS-G method is employed to achieve the final ranking results. The detailed descriptions of the major steps are elaborated in the following subsections.

Fuzzy AHP

AHP is developed by Saaty (1980), maybe it is one of the famous, dazzling and most widely used models in decision making. With the extension of this method in fuzzy set theory, fuzzy AHP was developed. In the proposed methodology, AHP with its fuzzy extension, namely fuzzy AHP, is applied to obtain more decisive judgments by prioritizing the market segment selection criteria and weighting them in the presence of
There are numerous fuzzy AHP applications in the literature that propose systematic approaches for selection of alternatives and justification of problem by using fuzzy set theory and hierarchical structure analysis (Efendigil et al. 2008; Önüt et al. 2010). DMs usually find it more convenient to express interval judgments than fixed value judgments due to the fuzzy nature of the comparison process (Bozdag et al. 2003). This study concentrates on a fuzzy AHP approach introduced by Chang (1992), in which triangular fuzzy numbers are preferred for pairwise comparison scale. Extent analysis method is selected for the synthetic extent values of the pairwise comparisons. Some papers published used the fuzzy AHP procedure based on extent analysis method and showed how it can be applied to selection problems (Cebeci, Ruan 2007; Kahraman et al. 2003, 2004). The outlines of the fuzzy sets and extent analysis method for fuzzy AHP are given below.

A fuzzy number is a special fuzzy set 

\[ F = \{(x, \mu_F(x)), \ x \in R\} \]

where \( x \) takes its values on the real line, \( R: -\infty \leq x \leq \infty \) and \( \mu_F(x) \) is a continuous mapping from \( R \) to the closed interval \([0,1]\). A triangular fuzzy number (TFN) expresses the relative strength of each pair of elements in the same hierarchy, and can be denoted as \( M = (l, m, u) \), where \( l \leq m \leq u \). The parameters \( l, m, u \) indicate the smallest possible value, the most promising value, and the largest possible value respectively in a fuzzy event. The recent applications of fuzzy AHP method, in short, are listed below:

- Keršulienė and Turskis (2011) used fuzzy AHP and ARAS for architect selection.
- Fouladgar et al. (2011) used fuzzy AHP and fuzzy TOPSIS for prioritizing strategies of the Iranian mining sector.
- Lin et al. (2011) used fuzzy Delphi method, fuzzy AHP and fuzzy theory to develop an evaluation system of knowledge management performance.
- Nepal et al. (2010) used fuzzy AHP approach to prioritization of CS attributes in target planning for automotive product development.
- Heo et al. (2010) used fuzzy AHP for analysis of the assessment factors for renewable energy dissemination program evaluation.
- Haghighi et al. (2010) applied fuzzy AHP to e-banking development in Iran.
- Gungor et al. (2009) used fuzzy AHP approach to personnel selection problem.

Triangular type membership function of \( M \) fuzzy number can be described as in Equation 1.

\[
\mu_M(x) = \begin{cases} 
0 & \text{if } x < l \\
(x - l)/(m - l) & \text{if } l \leq x \leq m \\
(u - x)/(u - m) & \text{if } m \leq x \leq u \\
0 & \text{if } x > u
\end{cases}
\]  

A linguistic variable is a variable whose values are expressed in linguistic terms (Önüt et al. 2008). The concept of a linguistic variable is very useful in dealing with situations, which are too complex or not well defined to be reasonably described in conventional quantitative expressions (Zadeh 1965; Zimmermann 1991; Kaufmann, Gupta 1991). In this study, the linguistic variables that are utilized in the model can be expressed in positive TFNs for each criterion as in Figure 1.
The linguistic variables matching TFNs and the corresponding membership functions are provided in Table 2. Proposed methodology employs a Likert Scale of fuzzy numbers starting from $\tilde{1}$ to $\tilde{9}$, symbolized with tilde ($\sim$) for the fuzzy AHP approach. Table 2 depicts AHP and fuzzy AHP comparison scale considering the linguistic variables that describes the importance of criteria and alternatives to improve the scaling scheme for the judgment matrices.

**Table 2.** Linguistic variables describing weights of the criteria and values of ratings

<table>
<thead>
<tr>
<th>Linguistic scale for importance</th>
<th>Fuzzy numbers for fuzzy AHP</th>
<th>Membership function</th>
<th>Domain</th>
<th>Triangular fuzzy scale $(l, m, u)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Just equal</td>
<td>$\tilde{1}$</td>
<td>$\mu_M(x) = (3 - x)/(3 - 1)$</td>
<td>$1 \leq x \leq 3$</td>
<td>$(1.0, 1.0, 1.0)$</td>
</tr>
<tr>
<td>Equal importance</td>
<td>$\tilde{1}$</td>
<td>$\mu_M(x) = (x - 1)/(3 - 1)$</td>
<td>$1 \leq x \leq 3$</td>
<td>$(1.0, 1.0, 3.0)$</td>
</tr>
<tr>
<td>Weak importance of one over another</td>
<td>$\tilde{3}$</td>
<td>$\mu_M(x) = (5 - x)/(5 - 3)$</td>
<td>$3 \leq x \leq 5$</td>
<td>$(1.0, 3.0, 5.0)$</td>
</tr>
<tr>
<td>Essential or strong importance</td>
<td>$\tilde{5}$</td>
<td>$\mu_M(x) = (x - 3)/(5 - 3)$</td>
<td>$3 \leq x \leq 5$</td>
<td>$(3.0, 5.0, 7.0)$</td>
</tr>
<tr>
<td>Very strong importance</td>
<td>$\tilde{7}$</td>
<td>$\mu_M(x) = (x - 5)/(7 - 5)$</td>
<td>$5 \leq x \leq 7$</td>
<td>$(5.0, 7.0, 9.0)$</td>
</tr>
<tr>
<td>Extremely preferred</td>
<td>$\tilde{9}$</td>
<td>$\mu_M(x) = (x - 7)/(9 - 7)$</td>
<td>$7 \leq x \leq 9$</td>
<td>$(7.0, 9.0, 9.0)$</td>
</tr>
</tbody>
</table>

By using TFNs via pairwise comparison, the fuzzy judgment matrix $\tilde{A}(a_{ij})$ can be expressed mathematically as in Equation 2:
The judgment matrix $\tilde{A}$ is a $n \times n$ fuzzy matrix containing fuzzy numbers $\tilde{a}_{ij}$.

$$\tilde{a}_{ij} = \begin{cases} 1, & i = j \\ 1, 3, 5, 7, 9 \text{ or } 1^{-1}, 3^{-1}, 5^{-1}, 7^{-1}, 9^{-1}, & i \neq j \end{cases}$$

Let $X = \{x_1, x_2, ..., x_n\}$ be an object set, whereas $U = \{u_1, u_2, ..., u_n\}$ is a goal set. According to fuzzy extent analysis, the method can be performed with respect to each object for each corresponding goal, $g_i$, resulting in $m$ extent analysis values for each object, given as $M_{gi}^1, M_{gi}^2, ..., M_{gi}^n$, $i=1,2, ..., n$ where all the $M_{gi}^j$ ($j=1,2, ..., m$) are TFNs representing the performance of the object $x_i$ with regard to each goal $u_j$. The steps of Chang’s extent analysis (1992) can be detailed as follows (Kahraman et al. 2003, 2004; Bozbura 2007):

**Step 1:** The fuzzy synthetic extent value with respect to the $i$th object is defined as:

$$S_i = \sum_{j=1}^{m} M_{gi}^j \otimes \left[ \sum_{i=1}^{n} \sum_{j=1}^{m} M_{gi}^j \right]^{-1}.$$  \hspace{1cm} (4)

To obtain $\sum_{j=1}^{m} M_{gi}^j$, perform the fuzzy addition operation $m$ extent analysis such that operation $m$ extent analysis values for a particular matrix will be as follows:

$$\sum_{j=1}^{m} M_{gi}^j = \left( \sum_{j=1}^{m} l_j, \sum_{j=1}^{m} m_j, \sum_{j=1}^{m} u_j \right),$$

then obtain $\left[ \sum_{i=1}^{n} \sum_{j=1}^{m} M_{gi}^j \right]^{-1}$, perform the fuzzy addition operation of $M_{gi}^j$ ($j=1,2, ..., m$) values as shown below:

$$\sum_{i=1}^{n} \sum_{j=1}^{m} M_{gi}^j = \left( \sum_{i=1}^{n} l_i, \sum_{i=1}^{n} m_i, \sum_{i=1}^{n} u_i \right),$$

then compute the inverse of the vector in Equation 6 as follows:

$$\left[ \sum_{i=1}^{n} \sum_{j=1}^{m} M_{gi}^j \right]^{-1} = \left( \frac{1}{\sum_{i=1}^{n} u_i}, \frac{1}{\sum_{i=1}^{n} m_i}, \frac{1}{\sum_{i=1}^{n} l_i} \right).$$

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Step 2: The degree of possibility of $M_2 \geq M_1$ is defined as:

$$V(M_2 \geq M_1) = \sup \left[ \min \left( \mu_{M_1}(x), \mu_{M_2}(y) \right) \right]_{x \geq y},$$

and it can be equivalently expressed as follows:

$$V(M_2 \geq M_1) = \text{hgt}(M_1 \cap M_2) = \mu_{M_2}(d) = \begin{cases} 1, & \text{if } (m_2 \geq m_1), \\ 0, & \text{if } (l_1 \geq u_2), \\ \frac{l_1 - u_2}{(m_2 - u_2) - (m_1 - l_1)}, & \text{otherwise}, \end{cases}$$

where $d$ is the ordinate of the highest intersection point $D$ between $\mu_{M_1}$ and $\mu_{M_2}$ (see Figure 2). To compare $M_1$ and $M_2$, both the values of $V(M_1 \geq M_2)$ and $V(M_2 \geq M_1)$ are required.

Step 3: The degree of possibility of a convex fuzzy number to be greater than $k$ convex fuzzy numbers $M_i (i = 1, 2, \ldots, k)$ can be defined by Equation 10.

$$V(M \geq M_1, M_2, \ldots, M_K) = V[M \geq M_1] \text{ and, } V[M \geq M_2] \text{ and... and,}$$

$$V[M \geq M_k] = \min \left( V[M \geq M_i] \right)_{i = 1, 2, \ldots, k}. \quad \text{ (10)}$$

Assume that:

$$d'(A_i) = \min \left( S_i \geq S_k \right), \quad \text{ (11)}$$

where: $k = 1, 2, \ldots, n; k \neq i$. Then, the weight vector is given by as in Equation 12:

$$W' = \left( d'(A_1), d'(A_2), \ldots, d'(A_n) \right)^T, \quad \text{ (12)}$$

Where $A_i (i = 1, 2, \ldots, n)$ has $n$ elements.

Step 4: The normalized weight vectors are defined as:

$$W = \left( d(A_1), d(A_2), \ldots, d(A_n) \right)^T, \quad \text{ (13)}$$

where $W$ is a non fuzzy number.

![Fig. 2. Intersection point “d” between two fuzzy numbers $M_1$ and $M_2$](image-url)
COPRAS-G METHOD

In order to evaluate the overall efficiency of an alternative, it is necessary to identify selection criteria, to assess information relating to these criteria, and to develop methods for evaluating the criteria to meet the participant’s needs. Decision analysis is concerned with the situation in which a decision-maker (DM) has to choose among several alternatives by considering a particular set of, usually conflicting criteria. For this reason Complex proportional assessment (COPRAS) method that was developed by Zavadskas and Kaklauskas (1996) can be applied. This method was applied to the solution of various problems in construction (Tupenaite et al. 2010; Ginevičius et al. 2008; Kaklauskas et al. 2010; Zavadskas et al. 2010). The most of alternatives under development always deal with vague future, and values of criteria cannot be expressed exactly. This MCDM problem should be determined not by exact criteria values, but by fuzzy values or by values in some intervals. Zavadskas et al. (2008) presented the main ideas of complex proportional assessment method with grey interval numbers (COPRAS-G) method. The idea of COPRAS-G method with criterion values expressed in intervals is based on the real conditions of decision making and applications of the Grey systems theory (Deng 1982; Deng 1988). The COPRAS-G method uses a stepwise ranking and evaluating procedure of the alternatives in terms of significance and utility degree.

The recent developments of decision making models based on COPRAS methods are listed below:

- Uzsilaityte and Martinaitis (2010) investigated and compared different alternatives for the renovation of buildings taking into account energy, economic and environmental criteria while evaluating impact of renovation measures during their life cycle;
- Chatterjee et al. (2011) presented materials selection model based on COPRAS and EVAMIX methods;
- Zavadskas et al. (2011) presented assessment of the indoor environment;
- Podvezko (2011) presented comparative analysis of MCDM methods (SAW and COPRAS);
- Hashemkhani Zolfani et al. (2011) presented forest roads locating using COPRAS-G method;
- Hashemkhani Zolfani et al. (2012) carried out research on quality control manager selection applying COPRAS-G method;

The procedure of applying the COPRAS-G method consists of the following steps (Zavadskas et al. 2009):

1. Selecting the set of the most important criteria, describing the alternatives.
2. Constructing the decision-making matrix $\otimes X$: 
\[ \otimes X = \begin{bmatrix} \otimes x_{11} & \cdots & \otimes x_{1m} \\ \otimes x_{21} & \cdots & \otimes x_{2m} \\ \vdots & \ddots & \vdots \\ \otimes x_{n1} & \cdots & \otimes x_{nm} \end{bmatrix} = \begin{bmatrix} x_{11}^{1'} x_{11} & x_{12}^{1'} x_{12} & \cdots & x_{1m}^{1'} x_{1m} \\ x_{21}^{1'} x_{21} & x_{22}^{1'} x_{22} & \cdots & x_{2m}^{1'} x_{2m} \\ \vdots & \vdots & \vdots & \vdots \\ x_{n1}^{1'} x_{n1} & x_{n2}^{1'} x_{n2} & \cdots & x_{nm}^{1'} x_{nm} \end{bmatrix}, \]

\[ j = 1, \ n, \ i = 1, \ m, \quad (14) \]

Here \( \otimes x_{ji} \) is determined by \( \otimes x_{ji} \) (the smallest value, the lower limit) and \( x_{ji} \) (the biggest value, the upper limit).

3. Determining significances of the criteria \( q_{ij} \).

4. Normalizing the decision-making matrix \( \otimes X \):

\[ \tilde{x} = \frac{x_{ji}}{1/2 \left( \sum_{j=1}^{n} x_{ji} + \sum_{j=1}^{n} \bar{x}_{ji} \right)} = \frac{2x_{ji}}{\sum_{j=1}^{n} x_{ji} + \sum_{j=1}^{n} \bar{x}_{ji}} \]

\[ \tilde{x} = \frac{\bar{x}_{ji}}{1/2 \left( \sum_{j=1}^{n} x_{ji} + \sum_{j=1}^{n} \bar{x}_{ji} \right)} = \frac{2\bar{x}_{ji}}{\sum_{j=1}^{n} x_{ji} + \sum_{j=1}^{n} \bar{x}_{ji}} \]

\[ j = 1, \ n; \ i = 1, \ m, \quad (15) \]

In formula (15), \( x_{ji} \) is the lower value of the criterion \( i \) in the alternative \( j \) of the solution; \( \bar{x}_{ji} \) is the upper value of the criterion \( i \) in the alternative \( j \) of the solution; \( m \) is the number of criteria; \( n \) is the number of the alternatives, compared. Then, the decision-making matrix is normalized:

\[ \otimes \tilde{X} = \begin{bmatrix} \tilde{x}_{11}^{1'} x_{11} & \tilde{x}_{12}^{1'} x_{12} & \cdots & \tilde{x}_{1m}^{1'} x_{1m} \\ \tilde{x}_{21}^{1'} x_{21} & \tilde{x}_{22}^{1'} x_{22} & \cdots & \tilde{x}_{2m}^{1'} x_{2m} \\ \vdots & \vdots & \vdots & \vdots \\ \tilde{x}_{n1}^{1'} x_{n1} & \tilde{x}_{n2}^{1'} x_{n2} & \cdots & \tilde{x}_{nm}^{1'} x_{nm} \end{bmatrix}. \]

\[ (16) \]

5. Calculating the weighted normalized decision matrix \( \otimes \tilde{X} \). The weighted normalized values \( \otimes \tilde{x}_{ji} \) are calculated as follows:

\[ \otimes \tilde{x}_{ji} = \otimes \tilde{x}_{ji} \cdot q_{i} \text{ or } \tilde{x}_{ji} = \tilde{x}_{ji} \cdot q_{i} \text{ and } \bar{x}_{ji} = \bar{x}_{ji} \cdot q_{i}, \]

\[ (17) \]

In formula (17), \( q_{i} \) is the significance of the \( i\text{-th} \) criterion.

Then, the normalized decision-making matrix is:

\[ \otimes \tilde{X} = \begin{bmatrix} \otimes \tilde{x}_{11} & \otimes \tilde{x}_{12} & \cdots & \otimes \tilde{x}_{1m} \\ \otimes \tilde{x}_{21} & \otimes \tilde{x}_{22} & \cdots & \otimes \tilde{x}_{2m} \\ \vdots & \vdots & \vdots & \vdots \\ \otimes \tilde{x}_{n1} & \otimes \tilde{x}_{n2} & \cdots & \otimes \tilde{x}_{nm} \end{bmatrix} = \begin{bmatrix} \tilde{x}_{11}^{1'} x_{11} & \tilde{x}_{12}^{1'} x_{12} & \cdots & \tilde{x}_{1m}^{1'} x_{1m} \\ \tilde{x}_{21}^{1'} x_{21} & \tilde{x}_{22}^{1'} x_{22} & \cdots & \tilde{x}_{2m}^{1'} x_{2m} \\ \vdots & \vdots & \vdots & \vdots \\ \tilde{x}_{n1}^{1'} x_{n1} & \tilde{x}_{n2}^{1'} x_{n2} & \cdots & \tilde{x}_{nm}^{1'} x_{nm} \end{bmatrix}. \]

\[ (18) \]
6. Calculating the sums $P_j$ of criterion values, whose larger values are more preferable:

$$P_j = \frac{1}{2} \sum_{i=1}^{k} \left( \hat{x}_{ji} + \bar{x}_{ji} \right)$$  \hspace{1cm} (19)

7. Calculating the sums $R_j$ of criterion values, whose smaller values are more preferable:

$$R_j = \frac{1}{2} \sum_{i=1}^{m} \left( \hat{x}_{ji} + \bar{x}_{ji} \right); \hspace{0.5cm} i = k, m.$$  \hspace{1cm} (20)

In formula (20), $(m-k)$ is the number of criteria which must be minimized.

8. Determining the minimal value of $R_j$ as follows:

$$R_{\text{min}} = \min_{j} R_j; \hspace{0.5cm} j = 1, n.$$  \hspace{1cm} (21)

9. Calculating the relative significance of each alternative $Q_j$ the expression is obtained:

$$Q_j = P_j + \frac{\sum_{j=1}^{n} R_j}{R_j \sum_{j=1}^{n} \frac{1}{R_j}}.$$  \hspace{1cm} (22)

10. Determining the optimal criterion $K$ by the formula:

$$K = \max_{j} Q_j; \hspace{0.5cm} j = 1, n.$$  \hspace{1cm} (23)

11. Determining the priority order of the alternatives.

12. Calculating the utility degree of each alternative by the formula:

$$N_j = \frac{Q_j}{Q_{\text{max}}} \times 100\%.$$  \hspace{1cm} (24)

Here $Q_j$ and $Q_{\text{max}}$ are the significances of the alternatives obtained from equation (22).

4. Case study

A real world case problem is selected in chair manufacturing company to illustrate the application of the proposed approach. The selected company is Nilper Company, which is one of the well-known brands in chair manufacturing industry in Iran. Nilper Company is a large-sized manufacturing enterprise, which is a recognized leader in chair manufacturing industry in Iran. Nilper Company currently offers more than 50 models of managerial, administrative, and clinical chairs based on customer needs and ergonomic standards. In recent years, there has been a steady growth in demand for many models of office chairs. Therefore, it was a matter of company’s policy to undertake marketing research in order to improve its design process based on the main customers’ wants for office chairs. Recently, this market research project was done and three segments were defined, which are denoted as SEG1, SEG 2 and SEG 3, respectively. Also, this company needs to evaluate and select obtained market segments for doing
other marketing activities. Consequently, the project team including R&D Manager, Marketing Manager, Sales Manager and two industrial engineers working for the company was constructed. At this point, the company needs to evaluate segments and select only one segment from them. So, the first criteria list based on McDonald and Dunbar (2004) for the market segment evaluation and selection was prepared. The number of criteria was very high and it was very difficult to evaluate all of them. So project team decided to choose some number of criteria for evaluating. Besides, they had to consider their company conditions, future plans, competitors, etc. For reducing the number of criteria and in order to select the most reasonable criteria, a questionnaire including all the first list criteria was designed. Then, the project team have been asked to give a rate to each of the criterion containing “not important at all”, “not very important”, “important”, “quite important” and “very important” which are the verbal representation of the 1–5 numeric scale respectively. Next, rank of each criterion was selected based on the geometric mean of each criterion in all questionnaires. In the end and based on these ranks, nine criteria were determined to perform the analysis. The nine criteria are: Degree of concentration, Laws and government agency regulations, Types of competitors, Contribution margins, Manufacturing process technology required, Complexity, Growth rate per year, Size, and Leveraging factors which are denoted as \( X_1, X_2, X_3, X_4, X_5, X_6, X_7, X_8, \) and \( X_9 \), respectively. Furthermore, project team decided about kind of each criterion based on situations of Iran market. After determining all selection criteria and alternatives, the paired comparisons for criteria list (see Table 3) were made by using the TFNs to tackle the ambiguities involved in the process of the linguistic assessment of the data. The project team filled this table, formed by reaching general agreement on questions related to the importance of the criteria and alternatives via Delphi technique as a group decision-making tool.

According to the weights in Table 3, Size, Growth rate per year and Types of competitor were three of the most important considered criteria.

5. Results

The aim of using fuzzy AHP is to determine importance weight of the criteria that will be employed in COPRAS-G method. Table 3 depicts the pairwise comparison matrix set by TFNs that matches linguistic statements of data. The fuzzy values of paired comparison were converted to crisp values via the Chang’s extent analysis as mentioned before. First, the fuzzy synthetic extent values were calculated by using Equation 4 with the help of Equations 5–7. Equations 8–9 were applied to express the degree of synthetic extent values. To have a weight vector given by as in Equation 12, Equations 10–11 were applied by comparing the fuzzy numbers. After normalizing weight vector defined as in Equation 13, the obtained priority weight vector of criteria is figured out in the last column of Table 3. After this stage, project team evaluated each segment according to each criterion and Table 4 was developed.
Table 3. Pairwise comparisons of selection criteria via TFN

<table>
<thead>
<tr>
<th></th>
<th>X₁</th>
<th>X₂</th>
<th>X₃</th>
<th>X₄</th>
<th>X₅</th>
<th>X₆</th>
<th>X₇</th>
<th>X₈</th>
<th>X₉</th>
<th>Priority weight (W)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Degree of concentration (X₁)</td>
<td>1,1,1</td>
<td>1,3,5</td>
<td>1,1,3</td>
<td>1/7,1/5,1/3</td>
<td>1/7,1/5,1/3</td>
<td>1,1,3</td>
<td>1/9,1/9,1/7</td>
<td>1/9,1/7,1/5</td>
<td>1/5,1/3,1</td>
<td>0.051</td>
</tr>
<tr>
<td>Laws and government agency regulations (X₂)</td>
<td>1/5,1/3,1</td>
<td>1,1,1</td>
<td>1/9,1/7,1/5</td>
<td>1/5,1/3,1</td>
<td>1,1,3</td>
<td>1,3,5</td>
<td>1/7,1/5,1/3</td>
<td>1,3,5</td>
<td>0.079</td>
<td></td>
</tr>
<tr>
<td>Types of competitor (X₃)</td>
<td>1/3,1,1</td>
<td>5,7,9</td>
<td>1,1,1</td>
<td>1,3,5</td>
<td>3,5,7</td>
<td>1,1,3</td>
<td>1,3,5</td>
<td>1,1,3</td>
<td>1/3,1,1</td>
<td>0.135</td>
</tr>
<tr>
<td>Contribution margins (X₄)</td>
<td>3,5,7</td>
<td>1,3,5</td>
<td>1/5,1/3,1</td>
<td>1,1,1</td>
<td>3,5,7</td>
<td>1/9,1/7,1/5</td>
<td>1/5,1/3,1</td>
<td>0.111</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Manufacturing process technology required (X₅)</td>
<td>3,5,7</td>
<td>1/5,1/3,1</td>
<td>1/7,1/5,1/3</td>
<td>1/7,1/5,1/3</td>
<td>1,1,1</td>
<td>3,5,7</td>
<td>1/9,1/7,1/5</td>
<td>1/5,1/3,1</td>
<td>0.111</td>
<td></td>
</tr>
<tr>
<td>Complexity (X₆)</td>
<td>1/3,1,1</td>
<td>1/3,1,1</td>
<td>1/3,1,1</td>
<td>3,5,7</td>
<td>1/7,1/5,1/3</td>
<td>1,1,1</td>
<td>1,3,5</td>
<td>1/5,1/3,1</td>
<td>1/3,1,1</td>
<td>0.108</td>
</tr>
<tr>
<td>Growth rate per year (X₇)</td>
<td>7,9,9</td>
<td>1/5,1/3,1</td>
<td>1/5,1/3,1</td>
<td>7,9,9</td>
<td>5,7,9</td>
<td>1/3,1,1</td>
<td>1,1,1</td>
<td>1/7,1/5,1/3</td>
<td>1/5,1/3,1</td>
<td>0.146</td>
</tr>
<tr>
<td>Size (X₈)</td>
<td>5,7,9</td>
<td>3,5,7</td>
<td>1/3,1,1</td>
<td>5,7,9</td>
<td>3,5,7</td>
<td>1,3,5</td>
<td>3,5,7</td>
<td>1,1,1</td>
<td>1,3,5</td>
<td>0.180</td>
</tr>
<tr>
<td>Leveraging factors (X₉)</td>
<td>1,3,5</td>
<td>1/5,1/3,1</td>
<td>1,1,3</td>
<td>5,7,9</td>
<td>1,1,3</td>
<td>1,3,5</td>
<td>1,3,5</td>
<td>1/5,1/3,1</td>
<td>1,1,1</td>
<td>0.124</td>
</tr>
</tbody>
</table>

\[ V(S_{C₁} \geq S_{C₂}, S_{C₃}, S_{C₄}, S_{C₅}, S_{C₆}, S_{C₇}, S_{C₈}, S_{C₉}) = 0.283 \]
\[ V(S_{C₂} \geq S_{C₁}, S_{C₃}, S_{C₄}, S_{C₅}, S_{C₆}, S_{C₇}, S_{C₈}, S_{C₉}) = 0.441; \]
\[ V(S_{C₃} \geq S_{C₁}, S_{C₂}, S_{C₄}, S_{C₅}, S_{C₆}, S_{C₇}, S_{C₈}, S_{C₉}) = 0.748; \]
\[ V(S_{C₄} \geq S_{C₁}, S_{C₂}, S_{C₃}, S_{C₅}, S_{C₆}, S_{C₇}, S_{C₈}, S_{C₉}) = 0.614; \]
\[ V(S_{C₅} \geq S_{C₁}, S_{C₂}, S_{C₃}, S_{C₄}, S_{C₆}, S_{C₇}, S_{C₈}, S_{C₉}) = 0.368; \]
\[ V(S_{C₆} \geq S_{C₁}, S_{C₂}, S_{C₃}, S_{C₄}, S_{C₅}, S_{C₇}, S_{C₈}, S_{C₉}) = 0.600; \]
\[ V(S_{C₇} \geq S_{C₁}, S_{C₂}, S_{C₃}, S_{C₄}, S_{C₅}, S_{C₆}, S_{C₈}, S_{C₉}) = 0.809; \]
\[ V(S_{C₈} \geq S_{C₁}, S_{C₂}, S_{C₃}, S_{C₄}, S_{C₅}, S_{C₆}, S_{C₇}, S_{C₉}) = 1.000; \]
\[ V(S_{C₉} \geq S_{C₁}, S_{C₂}, S_{C₃}, S_{C₄}, S_{C₅}, S_{C₆}, S_{C₇}, S_{C₈}) = 0.689. \]
Table 4. Initial decision-making matrix with the criteria values described in intervals

<table>
<thead>
<tr>
<th>(q_i)</th>
<th>Min</th>
<th>Min</th>
<th>Min</th>
<th>Max</th>
<th>Min</th>
<th>Min</th>
<th>Max</th>
<th>Max</th>
<th>Max</th>
</tr>
</thead>
<tbody>
<tr>
<td>(x_1)</td>
<td>0.051</td>
<td>0.079</td>
<td>0.135</td>
<td>0.111</td>
<td>0.066</td>
<td>0.108</td>
<td>0.146</td>
<td>0.180</td>
<td>0.124</td>
</tr>
</tbody>
</table>

It indicates the initial decision making matrix, with the criterion values described in intervals. For the weight of criteria, we used weights of the last column of Table 3. The initial decision making matrix has been normalized first as discussed in section COPRAS-G method. The normalized decision-making matrix is presented in Table 5.

Table 5. Normalized weighted decision making matrix

<table>
<thead>
<tr>
<th>(x_1)</th>
<th>(x_2)</th>
<th>(x_3)</th>
<th>(x_4)</th>
<th>(x_5)</th>
<th>(x_6)</th>
<th>(x_7)</th>
<th>(x_8)</th>
<th>(x_9)</th>
</tr>
</thead>
<tbody>
<tr>
<td>SEG 1</td>
<td>40 60</td>
<td>40 60</td>
<td>80 90</td>
<td>70 80</td>
<td>20 30</td>
<td>60 70</td>
<td>80 90</td>
<td>60 70</td>
</tr>
<tr>
<td>SEG 2</td>
<td>70 80</td>
<td>50 60</td>
<td>60 70</td>
<td>80 90</td>
<td>40 50</td>
<td>70 80</td>
<td>90 95</td>
<td>50 60</td>
</tr>
<tr>
<td>SEG 3</td>
<td>50 60</td>
<td>70 80</td>
<td>60 70</td>
<td>60 70</td>
<td>30 40</td>
<td>60 70</td>
<td>80 90</td>
<td>70 80</td>
</tr>
</tbody>
</table>

Table 6 summarizes the results. The higher degree means the better rank, so based on the results of Table 6, the ranking of the three segments is “SEG 3 > SEG 1 > SEG 2”.

Table 6. Evaluation of utility degree

<table>
<thead>
<tr>
<th>Segment</th>
<th>(P_j)</th>
<th>(R_j)</th>
<th>(Q_j)</th>
<th>(N_j)</th>
</tr>
</thead>
<tbody>
<tr>
<td>SEG 1</td>
<td>0.1825</td>
<td>0.1399</td>
<td>0.3359</td>
<td>98.52%</td>
</tr>
<tr>
<td>SEG 2</td>
<td>0.189</td>
<td>0.154</td>
<td>0.3284</td>
<td>96.38%</td>
</tr>
<tr>
<td>SEG 3</td>
<td>0.1937</td>
<td>0.146</td>
<td>0.3407</td>
<td>100%</td>
</tr>
</tbody>
</table>

\(P_j\) hybrid approach results indicate that the best alternative with the highest degree is the best segment for doing marketing activities. So, based on the proposed methodology, SEG 3 could be selected as the best segment for the problem of market segment evaluation and selection in the Nilper manufacturing company.
6. Conclusion

Market environment becomes more and more competitive and companies should make right decisions about marketing problems. One of the important problems is market segment evaluation and selection. Market segment evaluation and selection is a critical managerial marketing activity for all the companies. It helps a company choose its target segment or segments so that company can focus its competitive advantages, its resources, its opportunities and marketing strategies on effectively satisfying customers’ needs and wants. In this paper, a hybrid MCDM methodology based on fuzzy AHP and COPRAS-G method for selecting the most suitable market segment was proposed. Fuzzy AHP is used to calculate the weight of each criterion, and COPRAS-G method is proposed to prioritize market segments from the best to the worst ones. This application has indicated that the model can be efficiently used in evaluating and selecting segments. Although the application of the model proposed in this study is specific to market segment evaluation and selection, it can also be used with slight modifications in decision-making process.

Reference


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